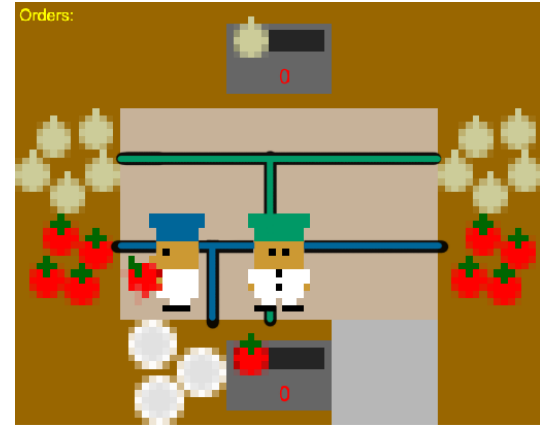
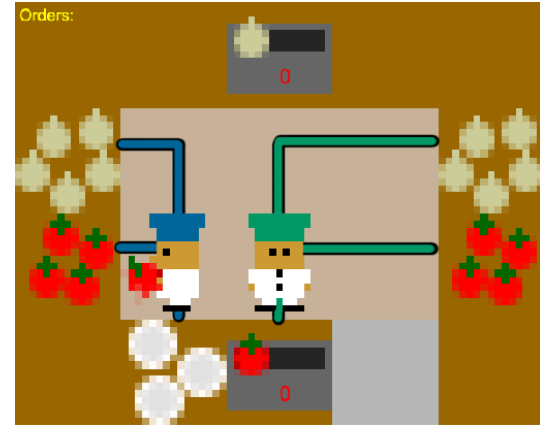


Motivation

MARL agents often converge to **arbitrary** conventions.



Split by ingredient



Split by side

Can we generate a **diverse set** of conventions to learn to work with people?

Diversity Definition

Want to **maximize nearest-neighbors score** for set of conventions, D :

$$S(D) = \mathbb{E}_{\pi \in D_{test}} [\max_{\pi^* \in D} J(\pi^*, \pi)]$$

For ad-hoc coordination, train a single **convention-aware agent**:

$$L(\hat{\pi}, D) = -J(\hat{\pi}, \hat{\pi}) - \frac{\lambda}{D} \sum_{\pi \in D} \mathbb{E}_{(o,a) \sim \pi} [\log(\hat{\pi}(a|o))]$$

To evaluate the performance of the convention-aware agent:

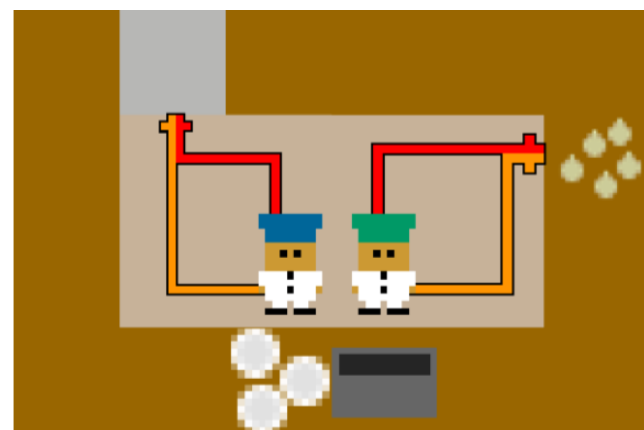
$$J(\hat{\pi}, D_{test}) = \mathbb{E}_{\pi \in D_{test}} [J(\hat{\pi}, \pi)]$$

Statistical Diversity

Some approaches add a term to **induce statistical variations** in trajectories:

$$C_{ADAP}(D) = \mathbb{E}_{s \in S} \left[\mathbb{E}_{\substack{\pi_1, \pi_2 \in D \\ \pi_1 \neq \pi_2}} \exp(-D_{KL}(\pi_1(s) \parallel \pi_2(s))) \right]$$

These fail to identify trivial variations in navigation:



Cross-Play Minimization

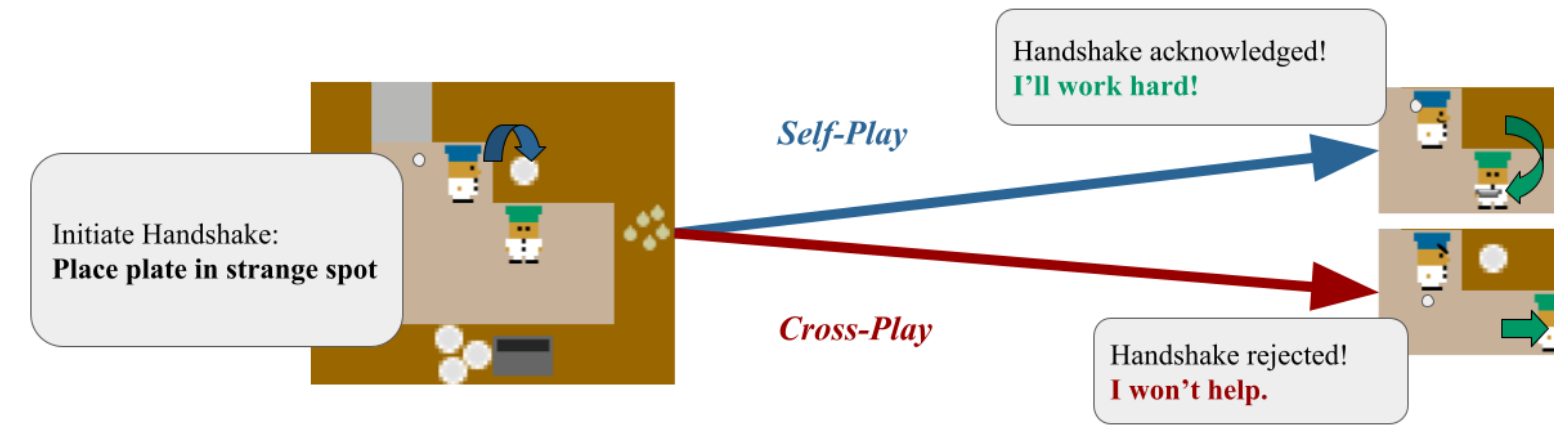
Adding a new convention π_n **guarantees an increase** in the score S :

$$S(D_n) \geq S(D_{n-1}) + p(\pi_n)(J(\pi_n, \pi_n) - \max_{\pi^* \in D_{n-1}} J(\pi_n, \pi^*))$$

Maximizing this lower bound gives a cross-play minimization algorithm.

Handshakes and Mixed-Play

Pure cross-play minimization **incentivizes sabotages** under cross-play.



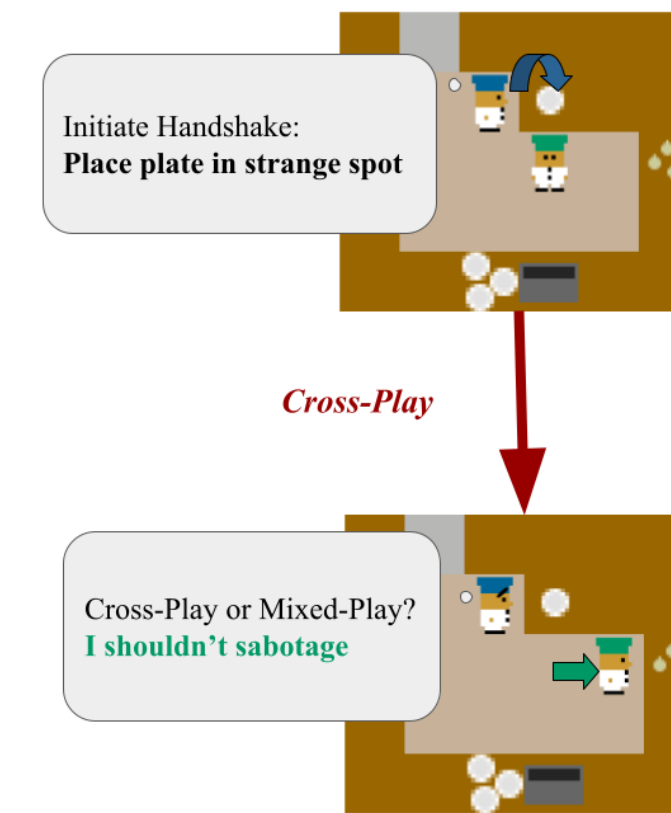
Mixed-play ensures that conventions always act in **good faith**.

Algorithm 1: Generating Mixed Play Buffer

Input: policies π_n, π^* , MDP M
Output: Replay buffer from running mixed-play.

```

1  $s_0, \bar{R} \leftarrow s, 0$ 
2  $t \sim \text{uniform}(1, T)$ 
3 for  $i \leftarrow [0, T)$  do
4    $o^1, o^2 \leftarrow o(s_i)$ 
5   if  $i < t$  then
6      $\pi_1^m \leftarrow \text{Randomly choose } \pi_n \text{ or } \pi^*$ 
7      $\pi_2^m \leftarrow \text{Randomly choose } \pi_n \text{ or } \pi^*$ 
8      $a_i^1, a_i^2 \leftarrow \pi_1^m(o^1), \pi_2^m(o^2)$ 
9      $s_{i+1}, - \leftarrow \text{Step in } M \text{ with } (a_i^1, a_i^2)$ 
10  else
11     $a_i^1, a_i^2 \leftarrow \pi_n(o^1), \pi_n(o^2)$ 
12     $s_{i+1}, r_i \leftarrow \text{Step in } M \text{ with } (a_i^1, a_i^2)$ 
Return:  $\text{ReplayBuffer}(s_{t:T}, a_{t:T}^1, a_{t:T}^2, r_{t:T})$ 
```



CoMeDi: Cross-Play and Mixed-Play

Loss function to generate convention π_n

$$L(\pi_n) = -J(\pi_n, \pi_n) + \alpha J(\pi_n, \pi^*) - \beta J_M(\pi_n, \pi^*)$$

Where π^* is the most-compatible previously discovered convention.

Algorithm 2: Diverse Conventions with CoMeDi

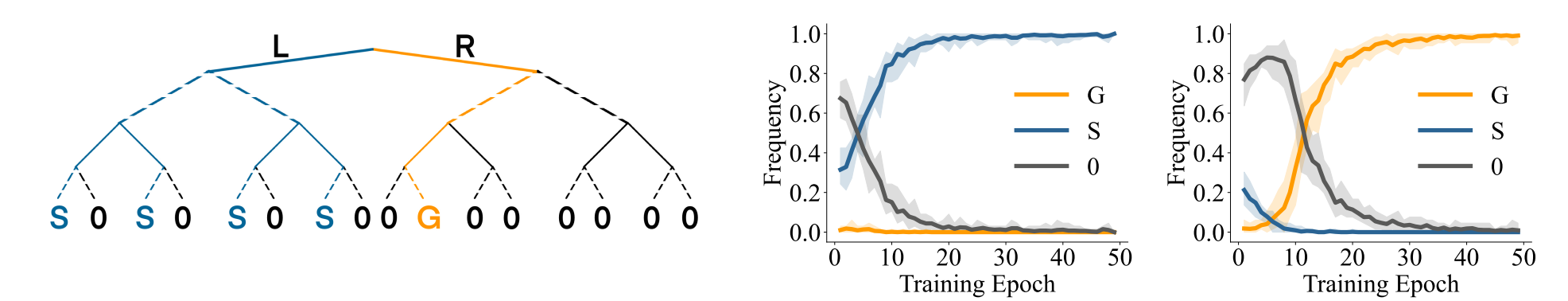
Input: Number of policies to generate n
Output: Diverse set of conventions D

```

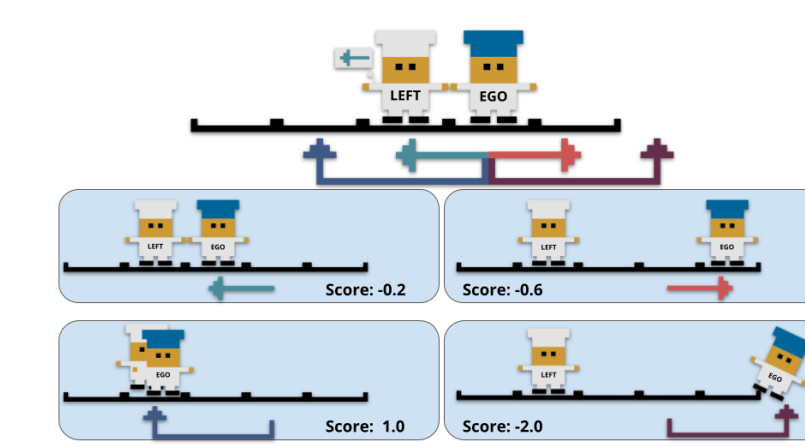
1  $D \leftarrow (\pi_1, \dots, \pi_n)$ , parameterized by  $(\theta_1, \dots, \theta_n)$ 
2 Train  $\pi_1$  with standard self-play
3 for  $i \in \{2, \dots, n\}$  do
4   while policy  $\pi_i$  has not converged do
5      $\pi^* \leftarrow \arg \max_{\pi^* \in D_{1:i-1}} J(\pi_i, \pi^*)$ 
6      $\tau_{SP} \leftarrow \text{GetRollout}(\pi_i, \pi_i)$ 
7      $\tau_{XP} \leftarrow \text{GetRollout}(\pi_i, \pi^*)$ 
8      $\tau_{MP} \leftarrow \text{MixedPlayRollout}(\pi_i, \pi^*)$ 
9     Estimate  $J(\pi_i, \pi_i), J(\pi_i, \pi^*), J_M(\pi_i, \pi^*)$  with  $\tau_{SP}, \tau_{XP}, \tau_{MP}$ 
10     $\theta_i \leftarrow \theta_i + \nabla_{\theta_i} [-J(\pi_i, \pi_i) + \alpha J(\pi_i, \pi^*) - \beta J_M(\pi_i, \pi^*)]$ 
Return:  $D$ 
```

Simulation Results

In Blind Bandits, CoMeDi finds both the **S** and **G** conventions:



In Balance Beam, tuning the mixed-play weight **eliminates handshakes**.



β	SP $\uparrow$	XP $\downarrow$	HS $\downarrow$	PX $\downarrow$	LS $\uparrow$	RS $\downarrow$
0.00	1.616	-0.392	0.16	0.00	1.128	-0.656
0.25	1.808	0.096	0.00	0.00	1.272	0.096
0.50	2.000	0.200	0.00	0.00	1.384	0.128
1.00	1.904	0.632	0.00	0.24	1.232	0.160

In Overcooked, CoMeDi's convention-aware agent has **strong cross-play** performance with held-out conventions.

layout	CoMeDi	XP	ADAP	SP	PPO_BC
simple	4.55	3.49	2.79	4.36	3.75
random1	3.42	1.58	0.72	2.70	2.29
random3	1.19	0.49	0.03	0.33	1.17
unident_s	5.27	3.62	1.84	2.51	2.58
random0	0.37	0.49	0.00	0.21	1.44

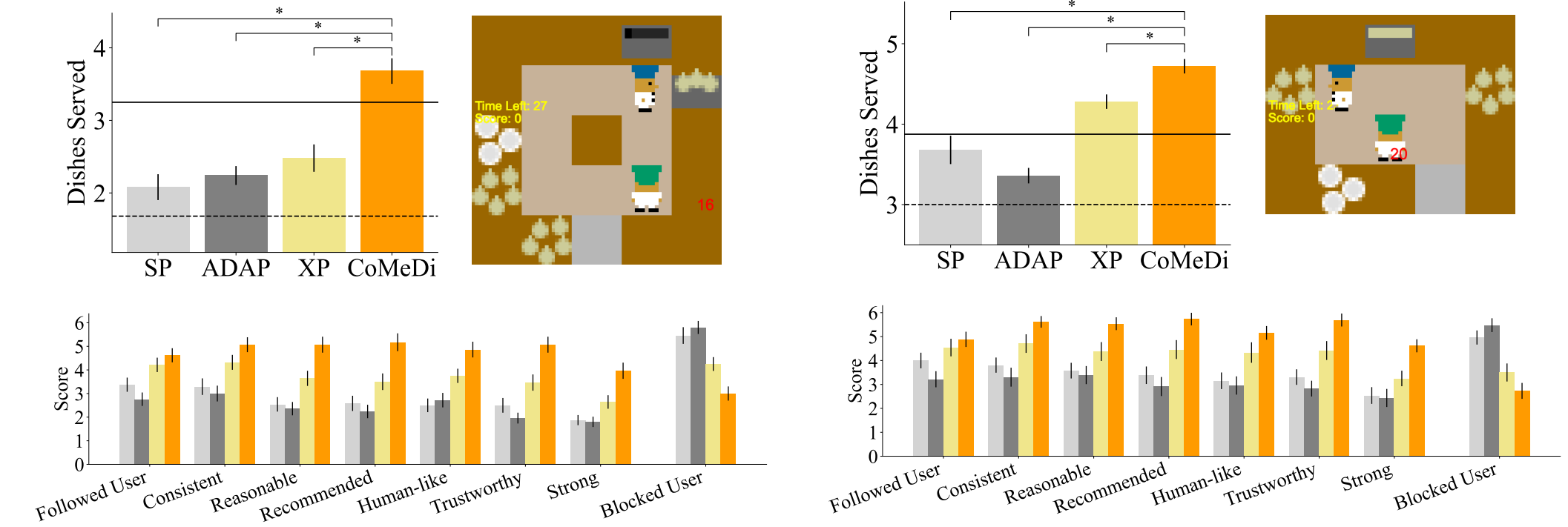
layout	CoMeDi	XP	ADAP	SP	PBT
simple	4.91	4.46	2.77	4.51	3.75
random1	3.43	1.81	1.10	2.38	2.29
random3	1.91	1.1	0.03	1.13	1.17
unident_s	2.94	3.16	2.59	4.52	2.58
random0	1.56	0.88	0	0.25	1.44

Scores with PBT

Scores with PPO_BC

Overcooked User Study

CoMeDi significantly outperforms baselines in terms of pure score and user opinion, even **surpassing human-level performance**.



Live Demo, Code, and Videos

Visit our website: <https://iliad.stanford.edu/Diverse-Conventions/>

